

Note: the distribution of these problems may not match the distribution of exam topics.

Problem §9.5 - 36(a,b): What is the congruence class $[4]_m$ when m is

- (a) 2?
- (b) 3?

Problem §10.2 - 5: Can a simple graph exist with 15 vertices each of degree five?

Problem §10.3 - 35,37-39,41-44: Determine whether the given pair of graphs is isomorphic (see Rosen for the graphs). Exhibit an isomorphism or provide a rigorous argument that none exists.

Problem §10.4 - 11a: Determine whether this graphs is strongly connected (see Rosen for the graphs) and if not, whether it is weakly connected.

Problem §10.4 - 37: Show that a simple graph with at least two vertices has at least two vertices that are not cut vertices.

Problem §10.5 - 10: Can someone cross all the bridges shown in this map (see Rosen) exactly once and return to the starting point?

Problem §10.5 - 36: Determine whether the given graph (see Rosen) has a Hamilton circuit.

Problem §10.6.18: Is a shortest path between two vertices in a weighted graph unique if the weights of edges are distinct?

Problem §10.7.15: If a connected planar simple graph has e edges and v vertices with $v \geq 3$ and no circuits of length three, prove that $e \leq 2v - 4$.

Problem §11.1.3 a-e: Answer these questions about the rooted tree illustrated (see Rosen!)

- (a) Which vertex is the root?
- (b) Which vertices are internal?
- (c) Which vertices are leaves?
- (d) Which vertices are children of j ?
- (e) Which vertex is the parent of h ?

Problem §11.2.1: Build a binary search tree for the words banana, peach, apple, pear, coconut, mango, and papaya using alphabetical order.