

*Note: the distribution of these problems may not match the distribution of exam topics.*

**Problem §9.1 - 42:** List the 16 different relations on the set  $A = \{0, 1\}$ .

**Problem §9.1 - 44(a,c,d,f):** Which of the 16 relations on  $A = \{0, 1\}$ , which you listed in Exercise 42, are reflexive? Symmetric? Antisymmetric? Transitive?

**Problem §9.3 - 6:** How can the matrix representing a relation  $R$  on a set  $A$  be used to determine whether the relation is asymmetric?

**Problem §9.3 - 13:** Let  $R$  be the relation represented by the matrix

$$M_R = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}.$$

Find the matrices representing  $R^{-1}$ ,  $\overline{R}$ ,  $R \circ R$ .

**Problem §9.5 - 36(a,b):** What is the congruence class  $[4]_m$  when  $m$  is

- (a) 2?
- (b) 3?

**Problem §10.2 - 5:** Can a simple graph exist with 15 vertices each of degree five?

**Problem §10.3 - 35,37-39,41-44:** Determine whether the given pair of graphs is isomorphic (see Rosen for the graphs). Exhibit an isomorphism or provide a rigorous argument that none exists.

**Problem §10.4 - 11a:** Determine whether this graph is strongly connected (see Rosen for the graphs) and if not, whether it is weakly connected.

**Problem §10.4 - 37:** Show that a simple graph with at least two vertices has at least two vertices that are not cut vertices.

**Problem §10.5 - 10:** Can someone cross all the bridges shown in this map (see Rosen) exactly once and return to the starting point?

**Problem §10.5 - 36:** Determine whether the given graph (see Rosen) has a Hamilton circuit.